

# MECANISME

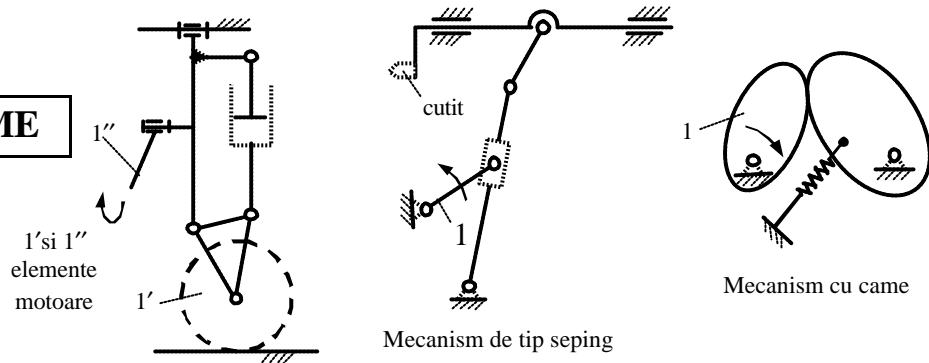


Figura 1.1

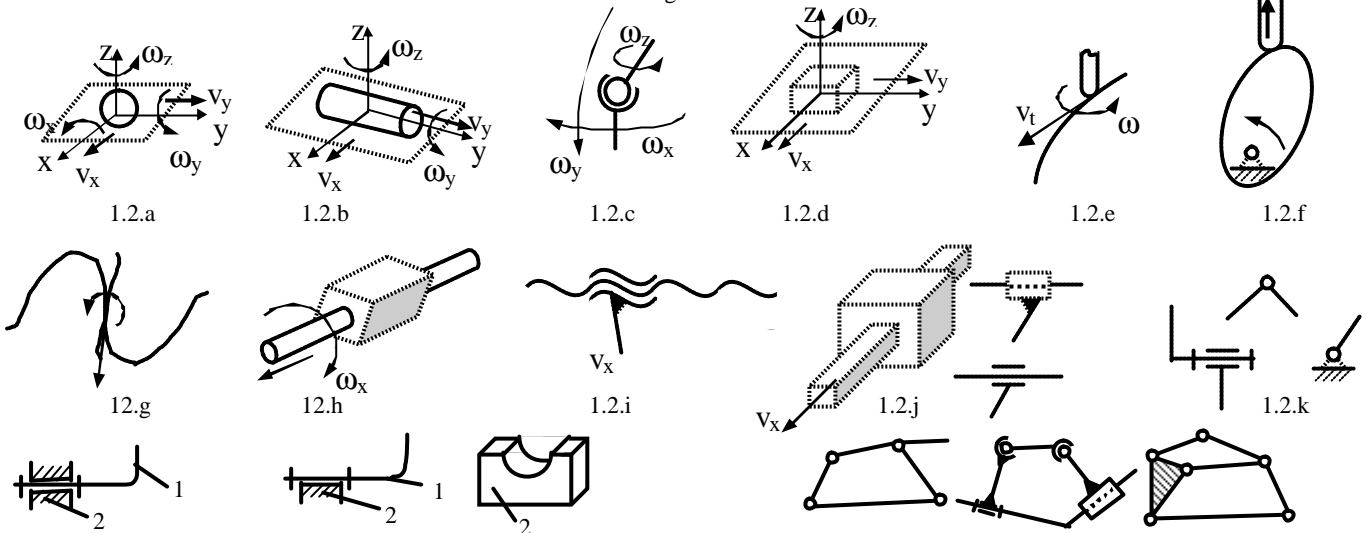


Figura 1.3.a

Figura 1.3.b

Figura 1.4

Clasificarea lanțurilor cinematice este prezentată în Tabelul 1.1. Rangul "j" al unui element este egal cu numărul cuplelor cinematice cu care acesta se leagă de alte elemente.

Tabelul 1.1

Dupa complexitatea miscarii	Lanturi cinematice plane	Toate elementele au miscari într-un singur plan sau în plane paralele
	Lanturi cinematice spatiale	Miscariile elementelor au loc în plane diferite
Dupa numarul cuplelor cinematice care revin unui element cinematic	Lanturi cinematice simple	Fiecare element are $j \leq 2$
	Lanturi cinematice complexe	Cel puțin un element are $j \geq 3$
	Lanturi cinematice închise	Toate elementele au $j \geq 2$
	Lanturi cinematice deschise	Cel puțin un element are $j = 1$

$$L = 6 \cdot n - \sum_{k=1}^5 k \cdot C_k \quad (1.1)$$

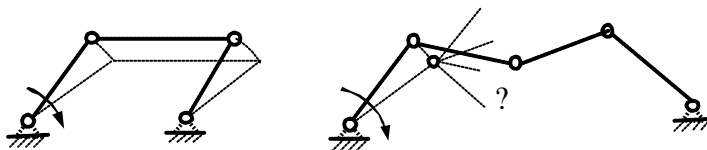


Figura 1.5

$$M = L - 6 = 6 \cdot (n - 1) - \sum_{k=1}^5 k \cdot C_k = 6 \cdot m - \sum_{k=1}^5 k \cdot C_k \quad (1.2)$$

$$L = (6 - 3) \cdot n - (5 - 3) \cdot C_5 - (4 - 3) \cdot C_4 \quad (1.3)$$

$$M = 3 \cdot m - 2 \cdot C_5 - C_4 \quad (1.4)$$

$$M = (6 - f) \cdot m - \sum_{k=1}^5 (k - f) \cdot C_k \quad (1.5)$$

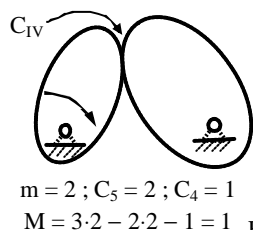
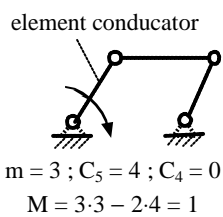
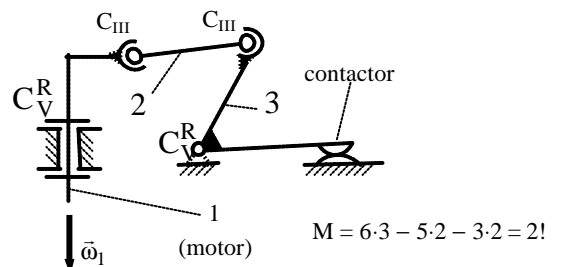


Figura 1.6



Mecanismul spatial schematizat în figura 1.7 are:  $m = 3$ ,  $C_5 = 2$ ,  $C_4 = 2$  și  $f = 1$ . Ca urmare, aplicând relația (1.5), rezulta  $M = 1$ .

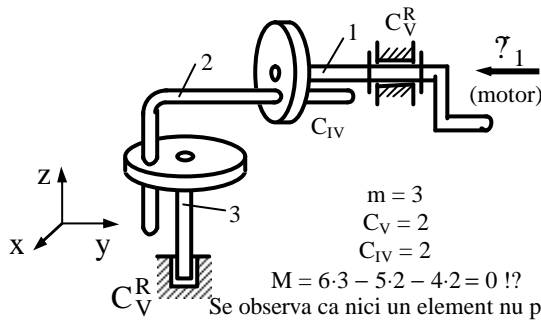


Figura 1.7

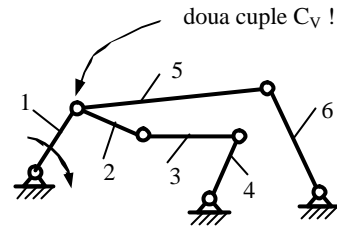
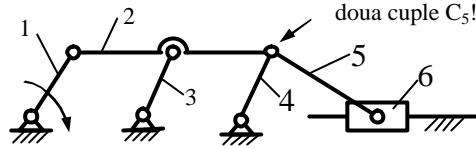


Figura 1.8



Elementul 3 este pasiv! Ajuta la rigidizarea barei 2.

Figura 1.9.a

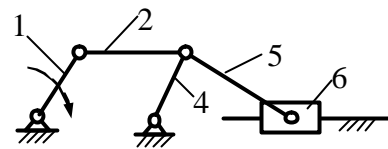


Figura 1.9.b

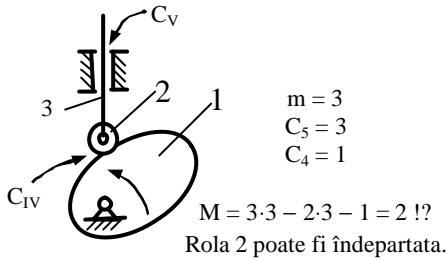


Figura 10.a

$$3 \cdot m_{ech} - 2 \cdot C_{5ech} = -1$$

$$C_{5ech} = \frac{3 \cdot m_{ech} + 1}{2}$$

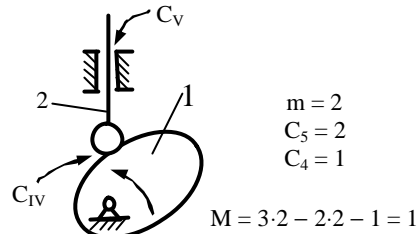


Figura 10.b

$$(1.6)$$

$$(1.7)$$

Tabelul 1.2

$m_{ech}$	1	3	5	7	...
$C_{5ech}$	2	5	8	11	...

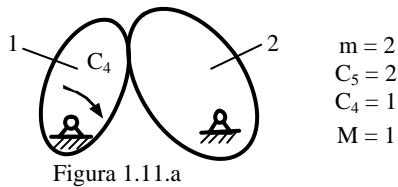


Figura 1.11.a

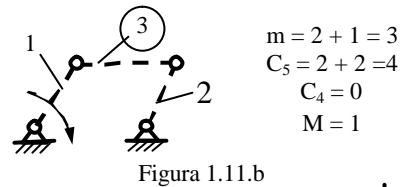


Figura 1.11.b

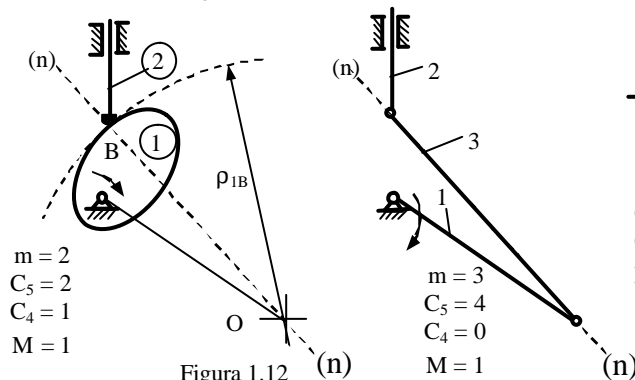


Figura 1.12

$$C_5 = \frac{3}{2}m$$

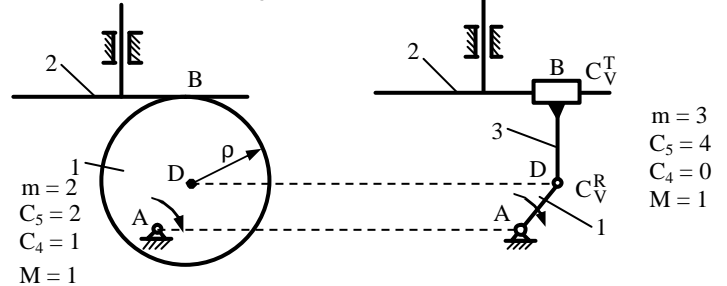
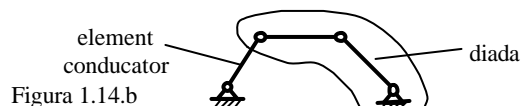
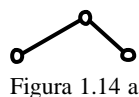


Figura 1.13

$$(1.8)$$

Tabelul 1.3

$m$	2	4	6	...
$C_5$	3	6	9	...



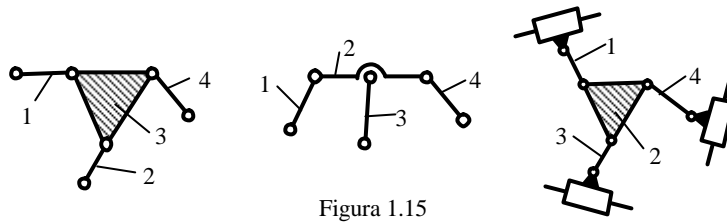


Figura 1.15

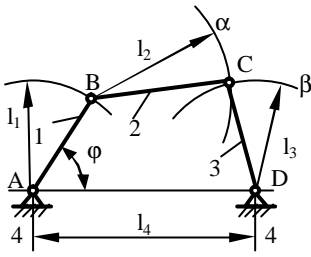


Figura 2.1

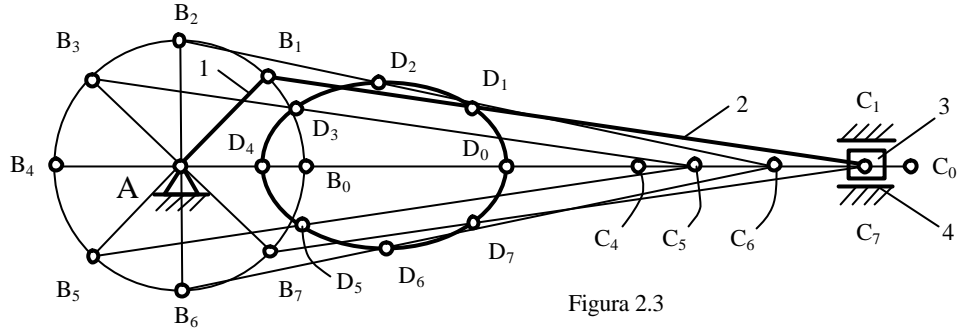


Figura 2.3

$$v_A = \omega \cdot l_{OA} \quad (2.1)$$

$$\frac{v_A}{l_{OA}} = \frac{K_v}{K_l} \cdot \frac{\overline{AV_A}}{OA} \quad (2.2)$$

$$\omega = \frac{K_v}{K_l} \cdot \text{tg}\phi = K_\omega \cdot \text{tg}\phi \quad (2.3)$$

$$K_\omega = 1 \text{ si deci } \omega = \text{tg}\phi \quad (2.4)$$

$$a_A^n = \frac{v_A^2}{r_A} = \omega^2 \cdot r_A \quad (2.5)$$

$$a_A^t = \varepsilon \cdot r_A \quad (2.6)$$

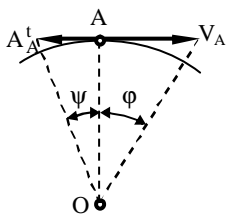


Figura 2.4

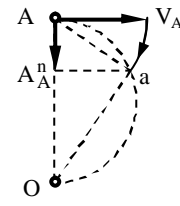


Figura 2.5

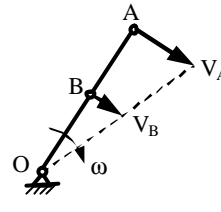


Figura 2.6

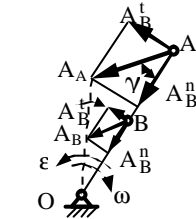


Figura 2.7

$$\varepsilon = \frac{a_A^t}{r_A} = \frac{K_a \cdot \overline{AA_A^t}}{K_l \cdot OA} = \frac{K_a}{K_l} \cdot \text{tg}\psi \quad (2.7)$$

$$\varepsilon = K_\varepsilon \cdot \text{tg}\psi \quad (2.7')$$

$$\varepsilon = \text{tg}\psi \quad (2.8)$$

$$\left(\overline{a_{AA}^n}\right)^2 = \overline{OA} \cdot \overline{AA_A^n}; \quad \overline{AA_A^n} = \frac{(\overline{AV_A})^2}{OA} = \frac{K_l}{K_v^2} \cdot \frac{v_A^2}{r_A} = \frac{K_l}{K_v^2} \cdot \overline{a_A^n} \quad (2.9)$$

sau  $\overline{a_A^n} = \frac{K_v^2}{K_l} \cdot \overline{AA_A^n}$ , adica vectorul  $\overline{AA_A^n}$  reprezinta acceleratia  $\overline{a_A^n}$  la scara  $K_a$ .

$$\overline{a_A} = \overline{a_A^n} + \overline{a_A^t} \quad (2.10)$$

$$a_A = \sqrt{(\overline{a_A^n})^2 + (\overline{a_A^t})^2} = \sqrt{\omega^4 \cdot l_{OA}^2 + \varepsilon^2 \cdot l_{OA}^2} = l_{OA} \cdot \sqrt{\omega^4 + \varepsilon^2} \quad (2.11)$$

$$a_B = l_{OB} \cdot \sqrt{\omega^4 + \varepsilon^2} \quad (2.12)$$

$$\text{tg}\gamma = \frac{a_A^t}{a_A^n} = \frac{r_A \cdot \varepsilon}{r_A \cdot \omega^2} = \frac{\varepsilon}{\omega^2} = \frac{a_B^t}{a_B^n} = \frac{r_B \cdot \varepsilon}{r_B \cdot \omega^2} = \frac{\varepsilon}{\omega^2} \quad (2.13)$$

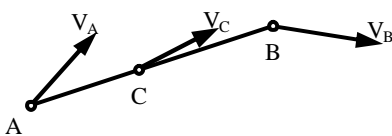


Figura 2.8

$$\overline{v_B} = \overline{v_A} + \overline{v_{BA}}$$

$$v_{BA} = \omega \cdot l_{AB}; \quad v_{BA} \perp AB$$

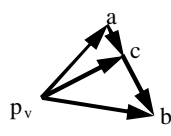


Figura 2.9

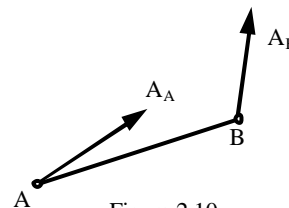


Figura 2.10

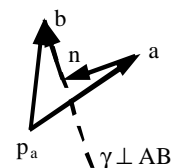


Figura 2.11

$$(2.14)$$

$$(2.15)$$

$$\bar{v}_C = \bar{v}_A + \bar{v}_{CA}, \text{ iar directia } \bar{v}_{CA} \perp AB. \quad (2.16)$$

$$\frac{ab}{ac} = \frac{AB}{AC} \quad (2.17)$$

$$\bar{a}_B = \bar{a}_A + \bar{a}_{BA} \quad (2.18)$$

$$\bar{a}_{BA} = \bar{a}_{BA}^n + \bar{a}_{BA}^t \quad (2.19)$$

$$\bar{a}_B = \bar{a}_A + \bar{a}_{BA}^n + \bar{a}_{BA}^t \quad (2.20)$$

$$\bar{a}_{BA}^n = \frac{v_{BA}^2}{l_{BA}} = \omega^2 \cdot l_{AB}; \quad \bar{a}_{BA}^n \parallel AB \quad (2.21)$$

$$\bar{a}_{BA}^t = \varepsilon \cdot l_{AB}; \quad \bar{a}_{BA}^t \perp AB \quad (2.22)$$

$$\bar{v}_A = K_v \cdot (\overline{p_v a})$$

$$v_B = K_v \cdot (\overline{p_v b}) \quad (2.23)$$

$$\bar{v}_{BA} = K_v \cdot (\overline{ab})$$

Pentru determinarea acceleratiilor se considera ecuatia vectoriala a acceleratiilor conform relatiei (2.18).

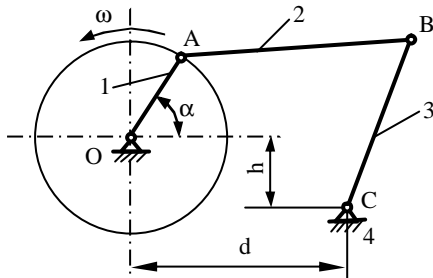


Figura 2.12

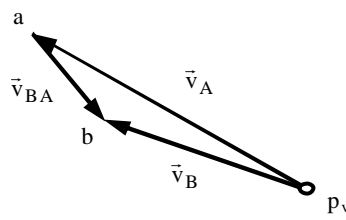


Figura 2.13

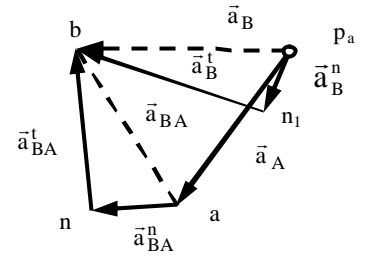


Figura 2.14

$$\bar{a}_B = \bar{a}_B^n + \bar{a}_B^t; \quad \bar{a}_A = \bar{a}_A^n + \bar{a}_A^t; \quad \bar{a}_{BA} = \bar{a}_{BA}^n + \bar{a}_{BA}^t \quad (2.24)$$

$$\bar{a}_B^n + \bar{a}_B^t = \bar{a}_A + \bar{a}_{BA}^n + \bar{a}_{BA}^t \quad (2.25)$$

$$\bar{a}_A^n = \frac{v_A^2}{l_1}; \quad \bar{a}_{BA}^n = \frac{v_{BA}^2}{l_2}; \quad \bar{a}_B^n = \frac{v_B^2}{l_3} \quad (2.26)$$

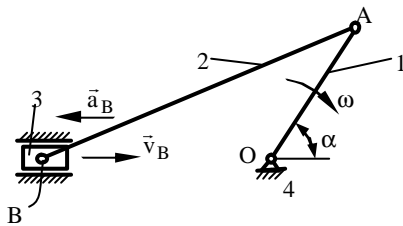


Figura 2.15

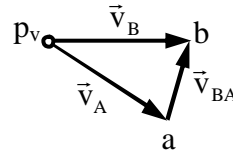


Figura 2.16

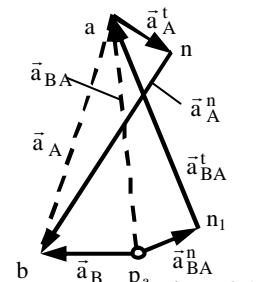


Figura 2.17

$$\bar{v}_{BA} = K_v \cdot (\overline{ab}); \quad \bar{v}_A = K_v \cdot (\overline{p_v a})$$

$$\bar{a}_B = \bar{a}_A + \bar{a}_A^t + \bar{a}_{BA}^n + \bar{a}_{BA}^t \quad (2.27)$$

$$\sum \bar{l}_n = 0 \quad (2.28)$$

$$\sum l_n \cdot e^{i\phi_n} = 0 \quad (2.29)$$

$$\sum (\dot{l}_n \cdot \omega_n \cdot e^{i\phi_n} + \dot{l}_n \cdot e^{i\phi_n}) = 0 \quad (2.30)$$

$$\sum (\dot{l}_n \cdot \dot{\omega}_n \cdot e^{i\phi_n} + i \cdot l_n \cdot \varepsilon_n \cdot e^{i\phi_n} - l_n \cdot \omega_n^2 \cdot e^{i\phi_n} + \ddot{l}_n \cdot e^{i\phi_n} + i \cdot \dot{l}_n \cdot \omega_n \cdot e^{i\phi_n}) = 0 \quad (2.31)$$

$$\sum (\dot{l}_n \cdot \varepsilon_n \cdot e^{i\phi_n} - l_n \cdot \omega_n^2 \cdot e^{i\phi_n} + 2 \cdot i \cdot \dot{l}_n \cdot \omega_n \cdot e^{i\phi_n} + \ddot{l}_n \cdot e^{i\phi_n}) = 0 \quad (2.32)$$

$$l_n \cdot e^{i\phi_n} = l_n \cdot \cos \phi_n + i \cdot l_n \cdot \sin \phi_n \quad (2.33)$$

$$\overline{O'O} + \overline{OA} + \overline{AB} = \overline{O'B} \text{ sau } \bar{h} + \bar{l}_1 + \bar{l}_2 = \bar{x}_B \quad (2.34)$$

$$\begin{cases} \bar{l}_1 \cdot \cos \phi_1 + \bar{l}_2 \cdot \cos \phi_2 = \bar{x}_B \\ h + l_1 \cdot \sin \phi_1 + l_2 \cdot \sin \phi_2 = 0 \end{cases} \quad (2.35)$$

$$\sin \phi_2 = -\frac{l_1 \cdot \sin \phi_1 + h}{l_2} \quad (2.36)$$

$$\left\{ \begin{aligned} -l_1 \cdot \sin \phi_1 \cdot \frac{d\phi_1}{dt} - l_2 \cdot \sin \phi_2 \cdot \frac{d\phi_2}{dt} &= \frac{dx_B}{dt} \\ l_1 \cdot \cos \phi_1 \cdot \frac{d\phi_1}{dt} + l_2 \cdot \cos \phi_2 \cdot \frac{d\phi_2}{dt} &= 0 \end{aligned} \right. \quad (2.37)$$

$$\frac{d\phi_1}{dt} = \omega_1; \quad \frac{d\phi_2}{dt} = \omega_2; \quad \frac{dx_B}{dt} = v_B \quad (2.39)$$

$$\begin{cases} -l_1 \cdot \omega_1 \cdot \sin \phi_1 - l_2 \cdot \omega_2 \cdot \sin \phi_2 = v_B \\ l_1 \cdot \omega_1 \cdot \cos \phi_1 + l_2 \cdot \omega_2 \cdot \cos \phi_2 = 0 \end{cases} \quad (2.40)$$

$$\omega_2 = -\omega_1 \cdot \frac{l_1 \cdot \cos \phi_1}{l_2 \cdot \cos \phi_2} \quad (2.41)$$

$$\begin{cases} -l_1 \cdot \omega_1 \cdot \cos \phi_1 \cdot \frac{d\phi_1}{dt} - l_1 \cdot \sin \phi_1 \cdot \frac{d\omega_1}{dt} - l_2 \cdot \omega_2 \cdot \cos \phi_2 \cdot \frac{d\phi_2}{dt} - l_2 \cdot \sin \phi_2 \cdot \frac{d\omega_2}{dt} = \frac{dv_B}{dt} \\ -l_1 \cdot \omega_1 \cdot \sin \phi_1 \cdot \frac{d\phi_1}{dt} + l_1 \cdot \cos \phi_1 \cdot \frac{d\omega_1}{dt} - l_2 \cdot \omega_2 \cdot \sin \phi_2 \cdot \frac{d\phi_2}{dt} + l_2 \cdot \cos \phi_2 \cdot \frac{d\omega_2}{dt} = 0 \end{cases} \quad (2.42)$$

$$\begin{cases} -l_1 \cdot \omega_1^2 \cdot \cos \phi_1 - l_2 \cdot \omega_2^2 \cdot \cos \phi_2 - l_2 \cdot \varepsilon_2 \cdot \sin \phi_2 = a_B \\ -l_1 \cdot \omega_1^2 \cdot \sin \phi_1 - l_2 \cdot \omega_2^2 \cdot \sin \phi_2 + l_2 \cdot \varepsilon_2 \cdot \cos \phi_2 = 0 \end{cases} \quad (2.43)$$

$$\varepsilon_2 = \frac{l_1 \cdot \omega_1^2 \cdot \sin \phi_1 + l_2 \cdot \omega_2^2 \cdot \sin \phi_2}{l_2 \cdot \cos \phi_2} \quad (2.44)$$

$$\sin \phi_2 = -\frac{l_1}{l_2} \cdot \sin \phi_1 \quad (2.45)$$

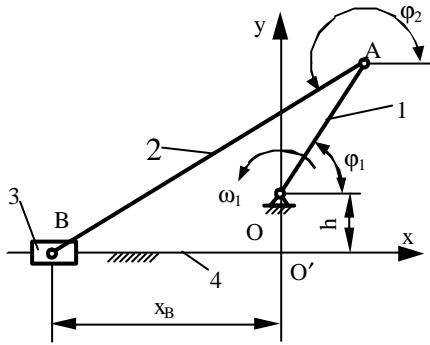


Figura 2.18

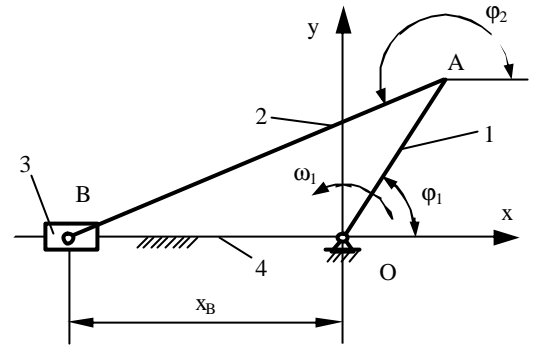


Figura 2.19

$$\tau_i = \begin{cases} \vec{F}_i = -m \cdot \vec{a}_G \\ \vec{M}_i = -J_G \cdot \vec{\varepsilon} \end{cases} \quad (3.1)$$

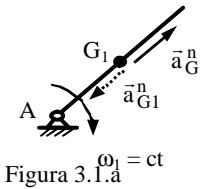


Figura 3.1.a

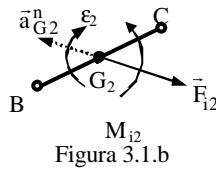


Figura 3.1.b

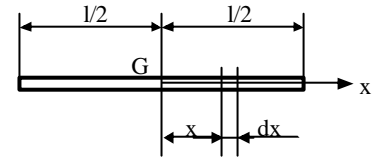


Figura 3.2

$$J_G = 2 \cdot \int_0^{l/2} x^2 dm \quad (3.2)$$

$$J_G = 2 \cdot m' \cdot \int_0^{l/2} x^2 dx = 2 \cdot m \cdot \frac{m' \cdot l^3}{12} \quad (3.3)$$

$$\tau_{io} = \begin{cases} \vec{F}_i = \int_m d\vec{F}_i \\ \vec{M}_i = \int_m \vec{r} \times d\vec{F}_i \end{cases} \quad (3.4)$$

$$\vec{F}_i = \int_m d\vec{F}_i = -\int_m \vec{a} \cdot dm = -\int_m (-\omega^2 \cdot \vec{\rho} + \vec{\varepsilon} \times \vec{\rho}) \cdot dm \quad (3.5)$$

$$\vec{F}_i = \omega^2 \cdot \int_m \vec{\rho} \cdot dm - \vec{\varepsilon} \times \int_m \vec{\rho} \cdot dm \quad (3.6)$$

$$\vec{M}_i = \int_m \vec{r} \times d\vec{F}_i = \int_m [(\vec{z} + \vec{\rho}) \times (\omega^2 \cdot \vec{\rho} - \vec{\varepsilon} \times \vec{\rho})] \cdot dm \quad (3.7)$$

$$\vec{M}_i = \omega^2 \cdot \int_m \vec{z} \times \vec{\rho} \cdot dm - \int_m \vec{z} \times (\vec{\varepsilon} \times \vec{\rho}) \cdot dm - \int_m \vec{\rho} \times (\vec{\varepsilon} \times \vec{\rho}) \cdot dm \quad (3.8)$$

$$\vec{M}_i = \vec{j} \cdot \omega^2 \cdot \int_m z \cdot x \cdot dm - \vec{i} \cdot \omega^2 \cdot \int_m y \cdot z \cdot dm + \vec{i} \cdot \varepsilon \cdot \int_m z \cdot x \cdot dm + \vec{j} \cdot \varepsilon \cdot \int_m y \cdot z \cdot dm - \vec{k} \cdot \varepsilon \cdot \int_m \rho^2 \cdot dm \quad (3.9)$$

$$\vec{M}_i = \vec{i} \cdot (-\omega^2 \cdot J_{yz} + \varepsilon \cdot J_{zx}) + \vec{j} \cdot (\omega^2 \cdot J_{zx} + \varepsilon \cdot J_{yz}) - \vec{k} \cdot \varepsilon \cdot J_z \quad (3.10)$$

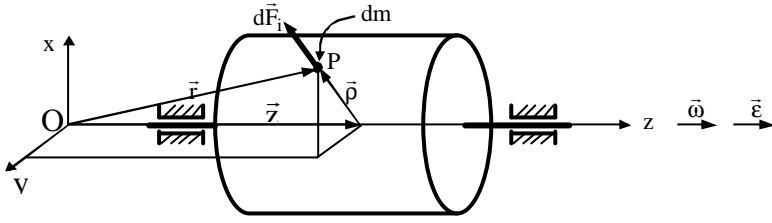


Figura 3.3

$$\vec{M}_i = \vec{i} \cdot M_{ix} + \vec{j} \cdot M_{iy} + \vec{k} \cdot M_{iz} \quad (3.11)$$

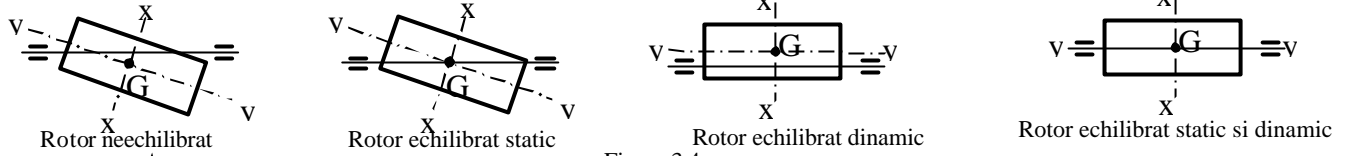


Figura 3.4

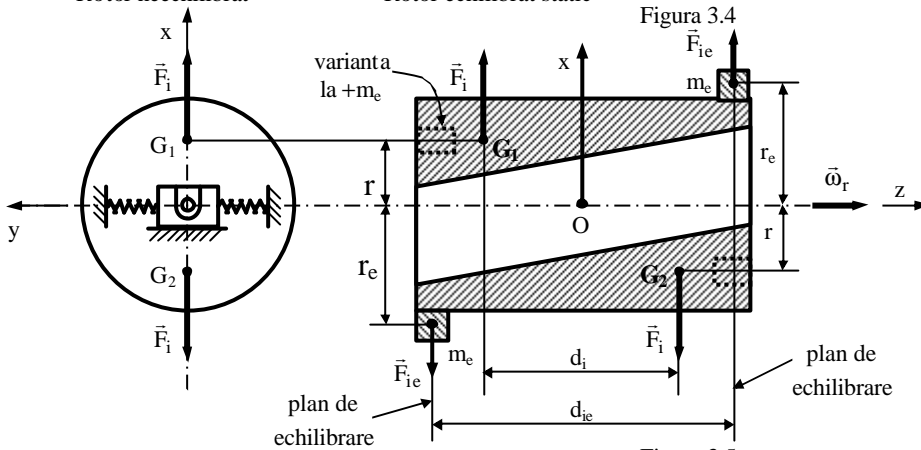


Figura 3.5

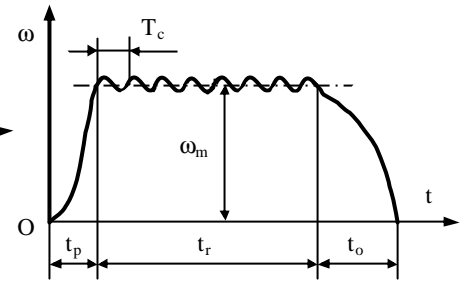


Figura 3.6

$$\sum \left( m_k \cdot \frac{v_{Gk2}^2}{2} - m_k \cdot \frac{v_{Gk1}^2}{2} \right) + \sum \left( J_k \cdot \frac{\omega_{k2}^2}{2} - J_k \cdot \frac{\omega_{k1}^2}{2} \right) = W_m - W_{ru} - W_{rp} \quad (3.12)$$

$$\sum m_k \cdot \frac{v_{Gk2}^2}{2} + \sum J_k \cdot \frac{\omega_{k2}^2}{2} = W_m - W_{ru} - W_{rp} \quad (3.13)$$

$$\sum m_k \cdot \frac{v_{Gk1}^2}{2} - \sum J_k \cdot \frac{\omega_{k1}^2}{2} = W_m - W_{ru} - W_{rp} \quad (3.14)$$

$$\eta = \frac{W_m - W_{rp}}{W_m} = 1 - \frac{W_{rp}}{W_m} \quad (3.15)$$

$$\eta = \frac{W_m}{W_m} = \eta_1 \cdot \eta_2 \cdots \eta_n = \prod \eta_i \quad (3.16)$$

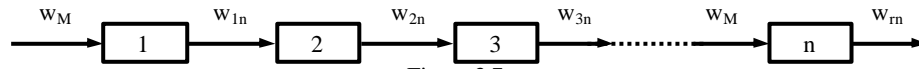


Figura 3.7

$$\sum \frac{m_k}{2} \cdot (v_{Gk2}^2 - v_{Gk1}^2) + \sum \frac{J_k}{2} \cdot (\omega_{k2}^2 - \omega_{k1}^2) = W_m - W_r \quad (3.17)$$

$$W_m = \sum \int_{l_{k1}}^{l_{k2}} F_{nk} \cdot \cos \alpha_k \cdot dl_k + \sum \int_{\varphi_{k1}}^{\varphi_{k2}} M_{nk} \cdot d\varphi_k \quad (3.18)$$

$$W_r = \sum \int_{l'_{k1}}^{l'_{k2}} F_{rk} \cdot \cos \alpha'_k \cdot dl'_k + \sum \int_{\varphi'_{k1}}^{\varphi'_{k2}} M_{rk} \cdot d\varphi'_k \quad (3.19)$$

$$F_{r,red} \cdot dl = \sum F_{rk} \cdot \cos \alpha'_k \cdot dl'_k + \sum M_{nk} \cdot d\varphi'_k \quad (3.20)$$

$$F_{m,red} = \sum F_{nk} \cdot \frac{v_k}{v'_B} \cdot \cos \alpha_k + \sum M_{nk} \cdot \frac{\omega_k}{v'_B} \quad (3.21)$$

$$F_{r,red} = \sum F_{rk} \cdot \frac{v'_k}{v'_B} \cdot \cos \alpha'_k + \sum M_{rk} \cdot \frac{\omega'_k}{v'_B} \quad (3.22)$$

$$M_{m.red.} \cdot d\varphi = \sum F_{nk} \cdot \cos \alpha_k \cdot dl_k + \sum M_{nk} \cdot d\varphi_k \quad (3.24)$$

$$M_{r.red.} \cdot d\varphi = \sum F_{rk} \cdot \cos \alpha'_k \cdot dl'_k + \sum M_{rk} \cdot d\varphi'_k \quad (3.25)$$

$$M_{m.red.} = \sum F_{mk} \cdot \frac{v_k}{\omega} \cdot \cos \alpha_k + \sum M_{mk} \cdot \frac{\omega_k}{\omega} \quad (3.26)$$

$$M_{m.red.} = \sum F_{rk} \cdot \frac{v'_k}{\omega} \cdot \cos \alpha'_k + \sum M_{rk} \cdot \frac{\omega'_k}{\omega} \quad (3.27)$$

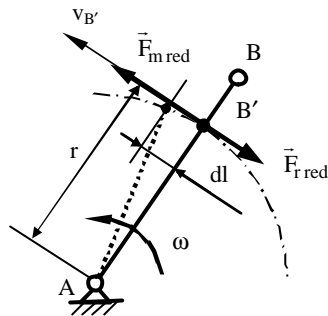


Figura 3.8

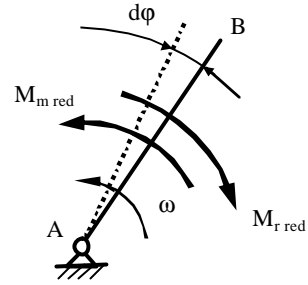


Figura 3.9

$$\frac{m_{red} \cdot v_{B'}^2}{2} = \sum \frac{m_k \cdot v_{Gk}^2}{2} + \sum \frac{J_k \cdot \omega_k^2}{2} \quad (3.28)$$

$$m_{red} = \sum m_k \cdot \left( \frac{v_{Gk}}{v_{B'}} \right)^2 + \sum J_k \cdot \left( \frac{\omega_k}{v_{B'}} \right)^2 \quad (3.29)$$

$$\frac{J_{red} \cdot \omega^2}{2} = \sum \frac{m_k \cdot v_{Gk}^2}{2} + \sum \frac{J_k \cdot \omega_k^2}{2} \quad (3.30)$$

$$J_{red} = \sum m_k \cdot \left( \frac{v_{Gk}}{\omega} \right)^2 + \sum J_k \cdot \left( \frac{\omega_k}{\omega} \right)^2 \quad (3.31)$$

$$\frac{m_{red2} \cdot v_{B'2}^2}{2} - \frac{m_{red1} \cdot v_{B'1}^2}{2} = \int_{l_1}^{l_2} (F_{m,red} - F_{r,red}) \cdot dl \quad (3.32)$$

$$v_{B'2} = \sqrt{\frac{2}{m_{m,red}} \cdot \int_{l_1}^{l_2} F_{red} \cdot dl + \frac{m_{red1} \cdot v_{B'1}^2}{m_{red2}}} \quad (3.33)$$

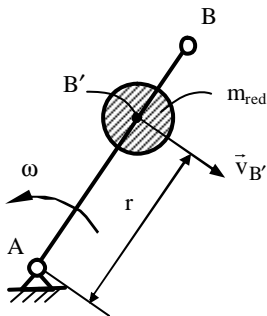


Figura 3.10

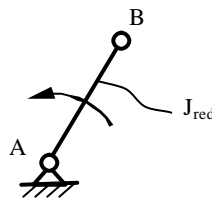


Figura 3.11

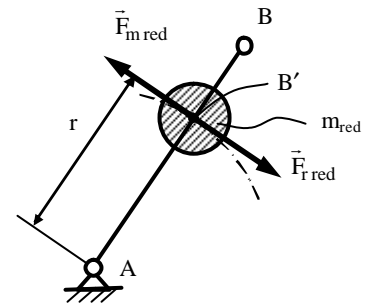


Figura 3.12

$$\omega_m = \frac{1}{\Delta\varphi} \cdot \int_{\varphi_1}^{\varphi_2} \omega \cdot d\varphi \quad (4.1)$$

Se definește gradul de neregularitate al mersului mașinii ( $\delta$ ) ca fiind  $\delta = \frac{\delta_{max} - \delta_{min}}{\delta_m}$ . Uzual, gradul de neregularitate al mersului mașinii are valorile:  $\delta = 1/5 \dots 1/30$  - pentru pompe;  $\delta = 1/20 \dots 1/5$  - pentru concașoare;  $\delta = 1/50 \dots 1/30$  - pentru mașini-unelte;  $\delta = 1/300 \dots 1/200$  - pentru motoare electrice de curent alternativ și  $\delta \leq 1/200$  pentru motoare de aviație.

Ca urmare, rezulta relațiile:  $\omega_{max} = \omega_m \cdot \left( 1 + \frac{\delta}{2} \right)$  și  $\omega_{min} = \omega_m \cdot \left( 1 - \frac{\delta}{2} \right)$ .

$$W_m = \int_0^{2\pi} M_{m,red} \cdot d\varphi \quad (4.2)$$

$$W_r = \int_0^{2\pi} M_{r,red} \cdot d\varphi \quad (4.3)$$

$$J_{\text{red.max}} \cdot \frac{\omega_{\text{max}}^2}{2} - J_{\text{red.min}} \cdot \frac{\omega_{\text{min}}^2}{2} = |\Delta W_{\text{max}}| \quad (4.4)$$

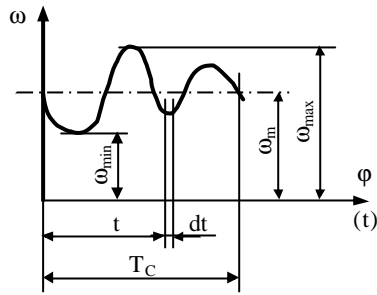


Figura 4.1

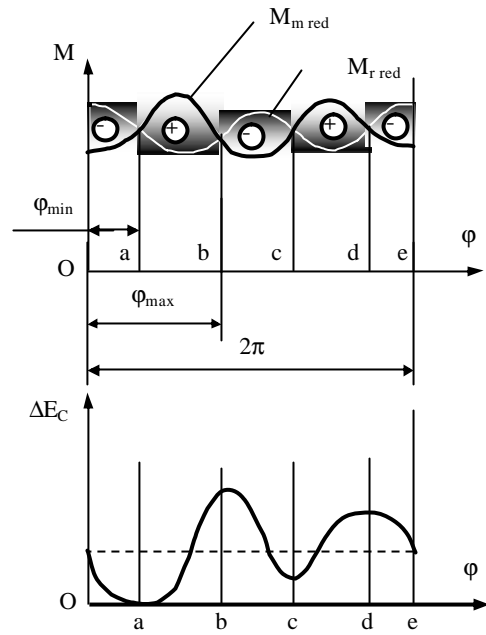


Figura 4.2

$$|\Delta W_{\text{max}}| = J_{\text{red}} \cdot \left( \frac{\omega_{\text{max}}^2}{2} - \frac{\omega_{\text{min}}^2}{2} \right) = J_{\text{red}} \cdot \omega_m^2 \cdot \delta \quad (4.5)$$

$$J_{\text{red}} = \frac{|\Delta W_{\text{max}}|}{\omega_m^2 \cdot \delta} \quad (4.6)$$

$$J_{\text{total}} = J = J_{\text{red}} + J_V \quad (4.7)$$

$$J_V = \frac{|\Delta W_{\text{max}}|}{\omega_m^2 \cdot \delta} - J_{\text{red}} \quad (4.8)$$

$$J_V \cong \frac{|\Delta W_{\text{max}}|}{\omega_m^2 \cdot \delta} \quad (4.9)$$

$$J = \frac{G \cdot D^2}{8 \cdot g} \quad (4.10)$$

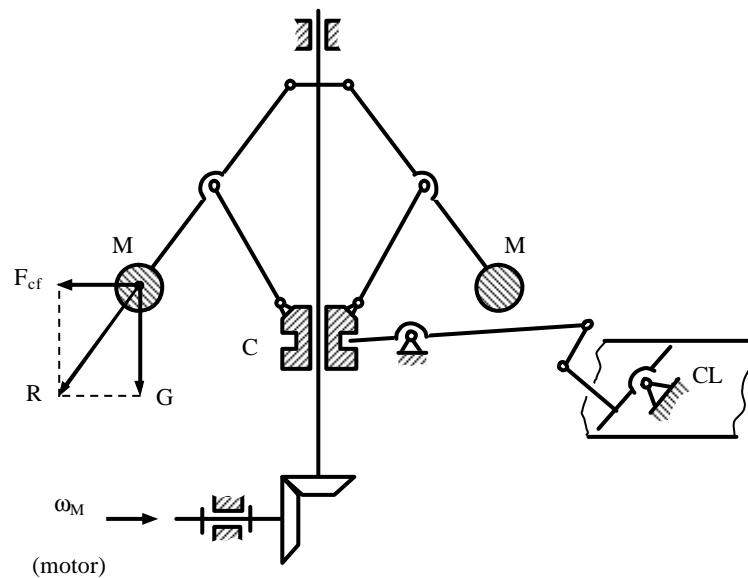


Figura 4.3



$$\phi = \arctg \frac{F_{f21}}{N_{21}} \quad (5.1)$$

$$p_m = \frac{N_{21}}{A_c} \leq p_a \quad (5.2)$$

$$\begin{cases} N = P \cdot \cos \beta + Q \cdot \cos \alpha \\ \mu \cdot N + Q \cdot \sin \alpha = P \cdot \sin \beta \end{cases} \quad (5.3)$$

$$P = P_{\max} = Q \cdot \frac{\sin(\alpha + \phi)}{\sin(\beta - \phi)} \quad (5.4)$$

$$P = P_{\min} = Q \cdot \frac{\sin(\alpha - \phi)}{\sin(\beta + \phi)} \quad (5.5)$$

$$\begin{cases} 2 \cdot \mu \cdot N \geq P \\ \mu \cdot N \cdot a + N \cdot l = P \cdot \left( d + \frac{a}{2} \right) \end{cases} \quad (5.6)$$

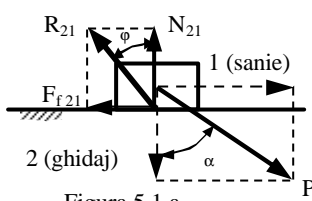


Figura 5.1.a

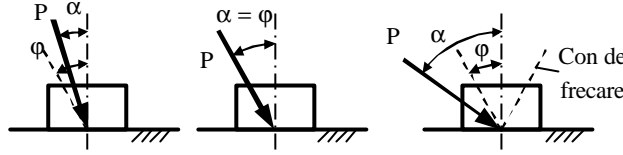


Figura 5.1.b

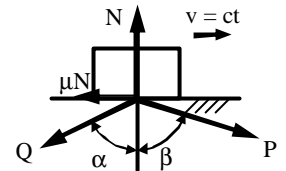


Figura 5.1.c

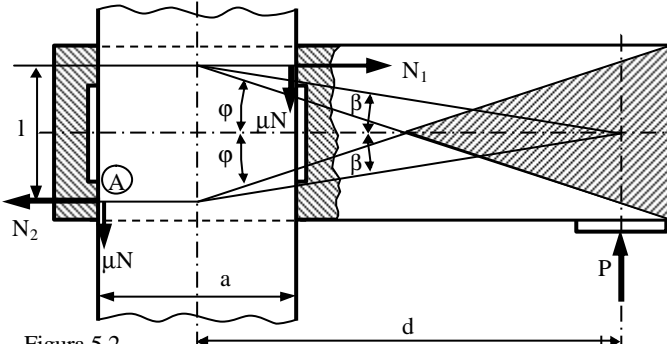


Figura 5.2

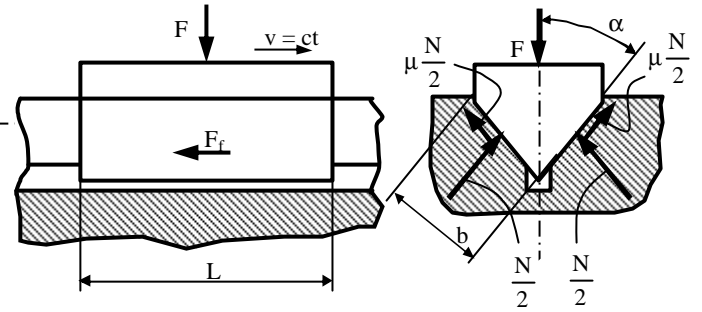


Figura 5.3

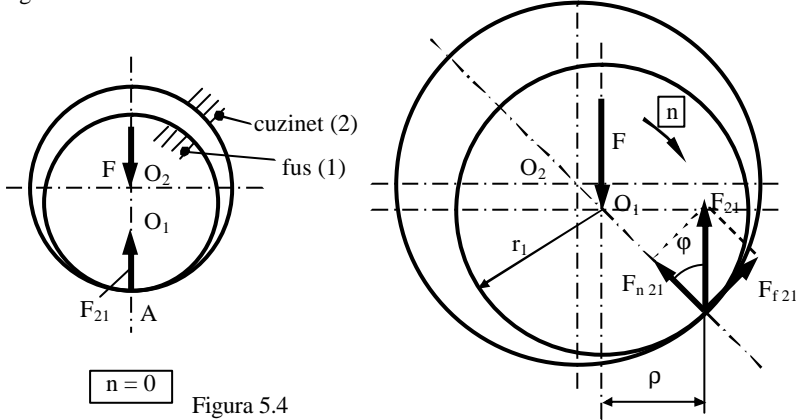


Figura 5.4

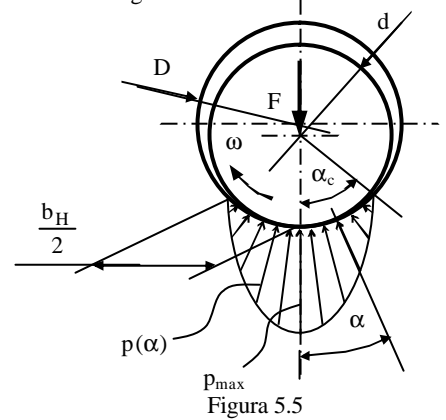


Figura 5.5

$$N = P \cdot \frac{2 \cdot d + a}{2 \cdot (l + \mu \cdot a)} \quad (5.7)$$

$$N = \frac{P}{2 \cdot \mu} \quad (5.8)$$

$$\mu \geq \frac{l}{2 \cdot d} \quad (5.9)$$

$$F = 2 \cdot \left( \frac{N}{2} \cdot \sin \alpha + \mu \cdot \frac{N}{2} \cdot \cos \alpha \right) \quad (5.10)$$

$$N = \frac{F}{\sin \alpha + \mu \cdot \cos \alpha} \quad (5.11)$$

$$p_m = \frac{N/2}{b \cdot L} \leq p_a \quad (5.12)$$

$$F_f = \mu \cdot N = \frac{\mu}{\sin \alpha + \mu \cdot \cos \alpha} \cdot F = \mu_c \cdot F \quad (5.13)$$

$$\mu_c = \frac{\mu}{\sin \alpha + \mu \cos \alpha} > \mu, \mu_c \text{ este minim pentru } \alpha = \frac{\pi}{2} - \varphi. \quad (5.14)$$

$$\rho = r_1 \cdot \sin \varphi \approx r_1 \cdot \operatorname{tg} \varphi = r_1 \cdot \mu = ct. \quad (5.15)$$

$$M_f = F_{f21} \cdot r_1 = F_{21} \cdot \sin \varphi \cdot r_1 \approx F \cdot \operatorname{tg} \varphi \cdot r_1 = F \cdot r_1 \cdot \mu \quad (5.16)$$

$$p(\alpha) = p_{\max} \cdot \sqrt{1 - \left(\frac{\alpha}{\alpha_c}\right)^2} \quad (5.17)$$

$$\sin \alpha_c = \sqrt{\frac{4}{\pi} \cdot \left(\frac{1 - \nu_1^2}{E_1} + \frac{1 - \nu_2^2}{E_2}\right)} \cdot \frac{2 \cdot F}{B \cdot (D - d)} \quad (5.18)$$

$$M_f = \int_{-\alpha_c}^{\alpha_c} \left[ \mu \cdot p(\alpha) \cdot B \cdot \frac{D}{2} \cdot d\alpha \right] \cdot \frac{D}{2} \quad (5.19)$$

$$M_f = \mu \cdot \frac{\alpha_c}{\sin \alpha_c} \cdot F \cdot \frac{D}{2} = \mu_{\text{ech}} \cdot F \cdot r, \text{ coeficientul de frecare conventional (echivalent): } \mu_{\text{ech}} = \frac{\mu \cdot \alpha_c}{\sin \alpha_c}. \quad (5.20)$$

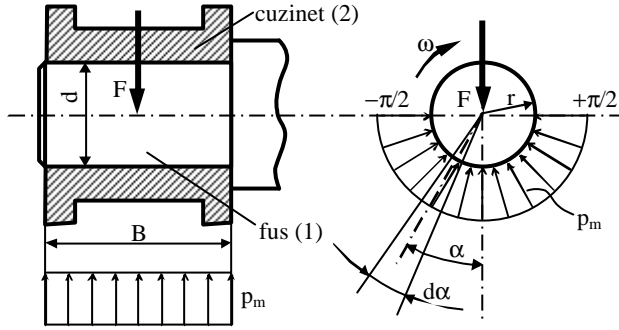


Figura 5.6

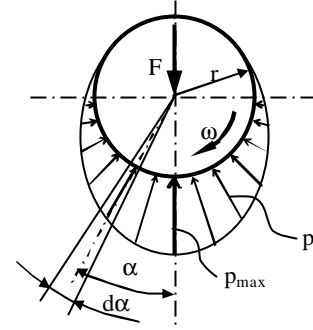


Figura 5.7

$$F = \int_{-\pi/2}^{\pi/2} p_m \cdot \left(\frac{d}{2} \cdot d\alpha\right) \cdot \cos \alpha \cdot B = p_m \cdot B \cdot d \quad (5.21)$$

$$p_m = \frac{F}{d \cdot B} \leq p_a \quad (5.22)$$

$$M_f = \int_{-\pi/2}^{\pi/2} \mu \cdot p_m \cdot \left(\frac{d}{2} \cdot d\alpha\right) \cdot B \cdot \frac{d}{2} = \mu \cdot \pi \cdot p_m \cdot \frac{d^2}{4} \cdot B \quad (5.23)$$

$$M_f = \frac{\pi}{2} \cdot \mu \cdot p_m \cdot r^2 \cdot B \quad (5.24)$$

$$M_f = \frac{\pi}{2} \cdot \mu \cdot F \cdot r \cong 1,57 \cdot \mu \cdot F_r \quad (5.25)$$

$$F = 2 \cdot p_{\max} \cdot \frac{d}{2} \cdot B \cdot \int_0^{\pi/2} \cos^2 \alpha \cdot d\alpha \quad (5.26)$$

$$p_{\max} = \frac{2 \cdot F}{\pi \cdot B \cdot r} \leq p_a \quad (5.27)$$

$$p_{\max} = \frac{4 \cdot F}{\pi \cdot B \cdot d} \leq p_a \quad (5.28)$$

$$M_f = \frac{\mu \cdot B \cdot d^2 \cdot p_{\max}}{2} \quad (5.29)$$

$$M_f = \frac{4}{\pi} \cdot \mu \cdot F \cdot r, P = F_f \cdot v = \mu \cdot F \cdot v \quad (5.30)$$

$(p_m \cdot v) \leq (p \cdot v)_{\text{admisibil}}$ , respectiv  $(p_{\max} \cdot v) \leq (p \cdot v)_{\text{admisibil}}$

$$p_m = \frac{4 \cdot F}{\pi \cdot (D_c^2 - D_i^2)} \leq p_a \quad (5.31)$$

$$M_f = \int_{\frac{D_i}{2}}^{\frac{D_c}{2}} (p_m \cdot 2\pi r \cdot dr) \cdot \mu \cdot r \quad (5.32)$$

$$M_f = \frac{1}{3} \cdot \mu \cdot F \cdot \frac{D_c^3 - D_i^3}{D_c^2 - D_i^2} \quad (5.33)$$

$$F = \int_{\frac{D_i}{2}}^{\frac{D_e}{2}} p \cdot 2\pi r \cdot dr = 2\pi(p\bar{r}) \cdot \int_{\frac{D_i}{2}}^{\frac{D_e}{2}} dr \quad (5.34)$$

$$F = 2 \cdot \pi \cdot (p \cdot \bar{r}) \cdot \frac{D_e - D_i}{2} \quad (5.35)$$

$$p = \frac{F}{\pi \cdot (D_e - D_i) \cdot \bar{r}}, \text{ pentru } r = D_i/2, p_{\max} = \frac{2 \cdot F}{\pi \cdot (D_e - D_i) \cdot D_i} \text{ si pentru } r = D_e/2 p_{\min} = \frac{2 \cdot F}{\pi \cdot (D_e - D_i) \cdot D_e} \quad (5.36)$$

$$M_f = \int_{\frac{D_i}{2}}^{\frac{D_e}{2}} (p \cdot 2\pi r \cdot dr) \cdot \mu \cdot r = 2\pi(p\bar{r}) \cdot \mu \cdot \int_{\frac{D_i}{2}}^{\frac{D_e}{2}} r \cdot dr \quad (5.37)$$

$$M_f = 2\pi\mu \cdot (p\bar{r}) \cdot \frac{D_e^2 - D_i^2}{8} = \frac{\pi}{4} \cdot \mu \cdot (p\bar{r}) \cdot (D_e^2 - D_i^2) \quad (5.38)$$

$$\text{Pentru } (p \cdot \bar{r}) = \frac{F}{\pi \cdot (D_e - D_i)} : M_f = \frac{1}{4} \cdot \mu \cdot F \cdot (D_e + D_i) \quad (5.39)$$

$$(p \cdot v) \leq (p \cdot v)_{\text{admisibil}}, \text{ respectiv } (p_{\max} \cdot v) \leq (p \cdot v)_{\text{admisibil}} \quad (5.40)$$

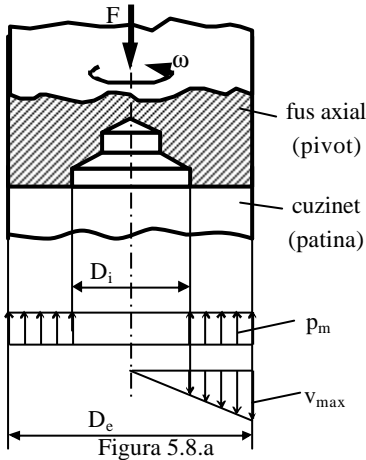


Figura 5.8.a

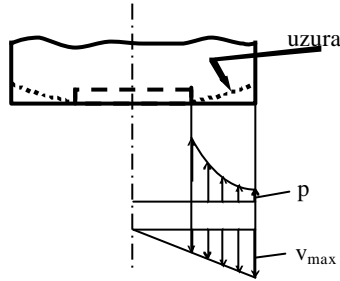


Figura 5.8.b

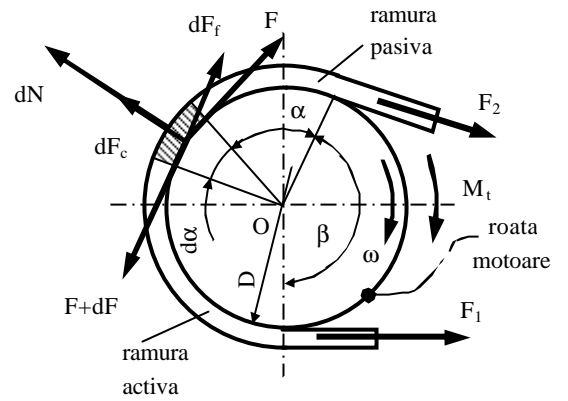


Figura 5.9

$$\begin{cases} dN + dF_c = (F + F + dF) \cdot \sin \frac{d\alpha}{2} \cong F \cdot d\alpha \\ dF_f = (F + dF - dF) \cdot \cos \frac{d\alpha}{2} \cong dF \end{cases} \quad \text{unde: } dF_f = \mu \cdot dN \text{ si } dF_c = r \cdot \omega^2 \cdot dm = r \cdot \frac{v^2}{r^2} \cdot r \cdot d\alpha \cdot B \cdot \rho \cdot s, \quad (5.41)$$

$$dF_f = B \cdot s \cdot \rho \cdot v^2 \cdot d\alpha \quad (5.42)$$

$$\frac{dF}{d\alpha} - \mu \cdot F = -\mu \cdot B \cdot s \cdot \rho \cdot v^2 \quad (5.43)$$

$$F = C \cdot e^{\mu \cdot \alpha} + B \cdot s \cdot \rho \cdot v^2 \quad (5.44)$$

$$\alpha = 0 \Rightarrow F = F_2 \Rightarrow C = F_2 - B \cdot s \cdot \rho \cdot v^2 \quad (5.45)$$

$$F = (F_2 - B \cdot s \cdot \rho \cdot v^2) \cdot e^{\mu \cdot \beta} + B \cdot s \cdot \rho \cdot v^2 \quad (5.46)$$

$$F_1 = (F_2 - B \cdot s \cdot \rho \cdot v^2) \cdot e^{\mu \cdot \beta} + B \cdot s \cdot \rho \cdot v^2 \quad (5.47)$$

$$F_u = \frac{2 \cdot M_t}{D} \quad (5.48)$$

$$F_u = F_1 - F_2 \quad (5.49)$$

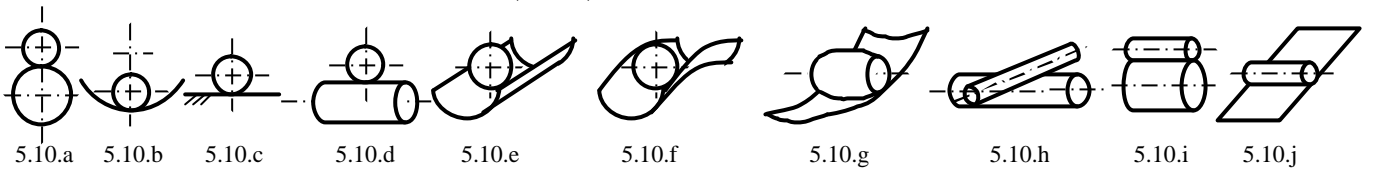
$$\begin{cases} F_1 = F_u \cdot \frac{e^{\mu \cdot \beta}}{e^{\mu \cdot \beta} - 1} + B \cdot s \cdot \rho \cdot v^2 \\ F_2 = F_u \cdot \frac{1}{e^{\mu \cdot \beta} - 1} + B \cdot s \cdot \rho \cdot v^2 \end{cases} \quad (5.50)$$

$$F_1 = \frac{F_u}{e^{\mu \cdot \beta} - 1} \cdot e^{\mu \cdot \beta} + B \cdot s \cdot \rho \cdot v^2 \quad (5.51)$$

$$p = \sigma_s = \frac{dN}{dA} = \frac{F \cdot d\alpha - dF_c}{B \cdot \left(\frac{D}{2}\right) \cdot d\alpha} = \frac{2 \cdot F_u}{B \cdot D \cdot (e^{\mu \cdot \beta} - 1)} \cdot e^{\mu \cdot \beta} \quad (5.52)$$

$$\text{Pentru } \alpha = \beta \Rightarrow p_{\max} = \sigma_{s\max} = \frac{2 \cdot F_u \cdot e^{\mu \cdot \beta}}{B \cdot D \cdot (e^{\mu \cdot \beta} - 1)} \quad (5.53)$$

Pentru  $\alpha = 0 \Rightarrow p_{\max} = \sigma_{s \max} = \frac{2 \cdot F_u}{B \cdot D \cdot (e^{\mu \beta} - 1)}$  (5.54)



$$F = \iint_S p_H \cdot dS = \int_{-b_H}^{b_H} p_H \cdot B \cdot db = \frac{\pi}{2} \cdot p_{H \max} \cdot b_H \cdot B \quad (5.55)$$

$$p_{H \max} = \sigma_{H \max} = \frac{2 \cdot F}{\pi \cdot b_H \cdot B} \quad (5.56)$$

$$b_H = \sqrt{\frac{4}{\pi} \cdot \frac{F \cdot \rho}{B} \cdot \left( \frac{1 - \nu_1^2}{E_1} + \frac{1 - \nu_2^2}{E_2} \right)} = \sqrt{\frac{8}{\pi} \cdot \frac{F \cdot \rho}{E_{ech} \cdot B}}, \text{ unde } \frac{1}{\rho} = \frac{1}{\rho_1} + \frac{1}{\rho_2} \quad (5.57)$$

$$E_{ech} = \frac{2}{\frac{1 - \nu_1^2}{E_1} + \frac{1 - \nu_2^2}{E_2}} \quad (5.58)$$

$$\sigma_{H \max} = \sqrt{\frac{F \cdot E_{ech}}{2 \cdot \pi \cdot \rho \cdot B}} \quad (5.59)$$

În cazul particular cilindru/plan,  $\rho_1 = R, \rho_2 \rightarrow \infty, E_1 = E$  si, ipotetic,  $E_2 \rightarrow \infty$ . Ca urmare,  $E_{ech} = \frac{2}{2 \cdot \frac{1 - \nu^2}{E}}$

$$b_H = 1,076 \cdot \sqrt{\frac{F \cdot R}{E \cdot B}} \quad (5.60)$$

$$\sigma_H = 0,418 \cdot \sqrt{\frac{F \cdot E}{R \cdot B}} \quad (5.61)$$

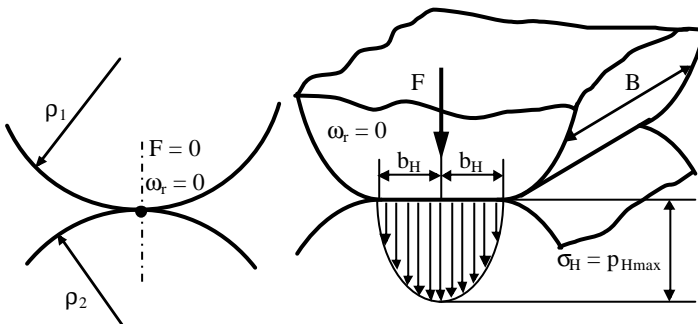


Figura 5.11

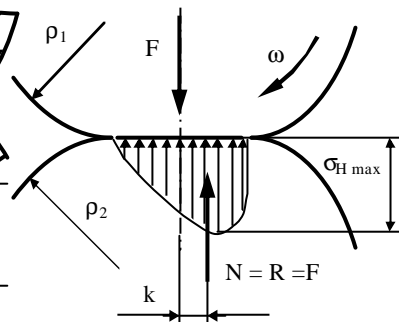


Figura 5.12

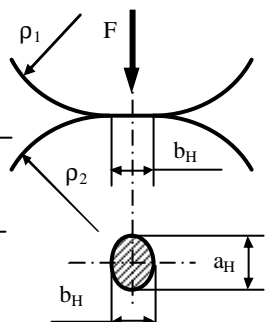


Figura 5.13

$$a_H = b_H = \sqrt[3]{\frac{3}{2} \cdot \frac{\eta \cdot F}{\sum k}} \text{ unde } \sum k = \frac{1}{\rho_1} + \frac{1}{\rho_2}, \eta = \frac{1 - \nu_1^2}{E_1} + \frac{1 - \nu_2^2}{E_2} \quad (5.62)$$

$$\sigma_{H \max} = \frac{1}{\pi} \cdot \sqrt[3]{\frac{3}{2} \cdot \left( \frac{\sum k}{\eta} \right)^2 \cdot F} \quad (5.63)$$

$$P_{fi} = P_{fiA} + P_{fiB} = F_i \cdot k \cdot \omega_1 \cdot \left( 1 + 2 \cdot \frac{\omega_b}{\omega_1} \right) \quad (5.64)$$

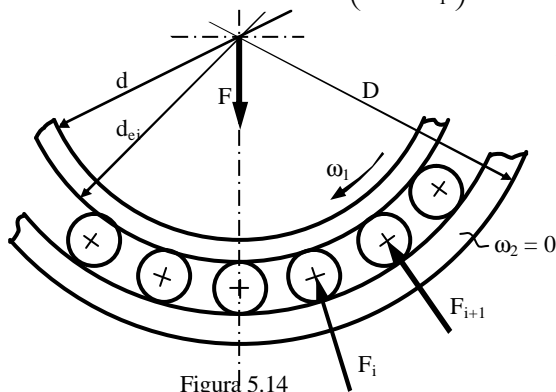


Figura 5.14

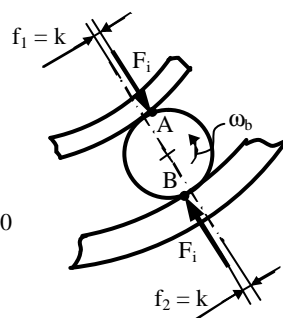


Figura 5.15

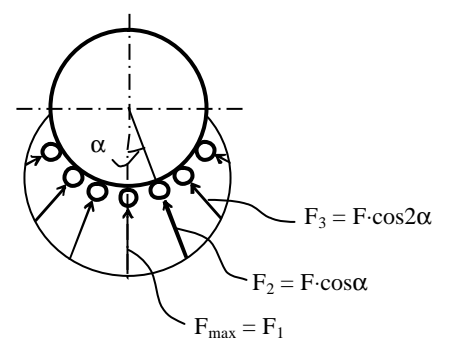


Figura 5.15

$$P_{fi} = F_i \cdot k \cdot \omega_1 \cdot \left(1 + 2 \cdot \frac{d_{ei}}{2 \cdot d_b}\right) = F_i \cdot k \cdot \omega_1 \cdot \left(1 + \frac{d_{ei}}{d_b}\right) \quad (5.65)$$

$$M_{fi} = \frac{P_{fi}}{\omega_1} = F_i \cdot k \cdot \left(1 + \frac{d_{ei}}{d_b}\right). \text{Momentul de frecare total } M_f = \sum M_{fi} = k \cdot \left(1 + \frac{d_{ei}}{d_b}\right) \cdot \sum F_i \quad (5.66)$$

$$\sum F_i = \frac{4}{\pi} \cdot F \quad (5.67)$$

$$M_f = \frac{4}{\pi} \cdot k \cdot F \cdot \left(1 + \frac{d_{ei}}{d_b}\right) \quad (5.68)$$

$$M_f = \frac{4}{\pi} \cdot k \cdot F \cdot \frac{d}{2} \cdot \left(1 + \frac{d_{ei}}{d_b}\right) \cdot \frac{2}{d} \quad (5.69)$$

$$\mu_r = \frac{8}{\pi} \cdot \frac{k}{d} \cdot \left(1 + \frac{d_{ei}}{d_b}\right) \ll \mu_a \quad (5.70)$$

$$M_f = \mu_r \cdot F \cdot \frac{d}{2} \quad (5.71)$$

$$\begin{cases} P_{fi} = 2F_i \cdot k \cdot \omega_b \\ \omega_b \cdot d_b = \omega_1 \cdot \frac{d_m}{2} \end{cases} \quad (5.72)$$

$$P_{fi} = F_i \cdot k \cdot \omega_1 \cdot \frac{d_m}{d_b} \quad (5.73)$$

$$M_f = \frac{\sum P_{fi}}{\omega_1} = k \cdot \frac{d_m}{d_b} \cdot \sum F_i \quad (5.74)$$

$$M_f = k \cdot F \cdot \frac{d_m}{d_b} = \mu_r \cdot F \cdot \frac{d}{2} \quad (5.75)$$

$$\mu_r = \frac{2 \cdot k \cdot d_m}{d \cdot d_b} \ll \mu_a \quad (5.76)$$

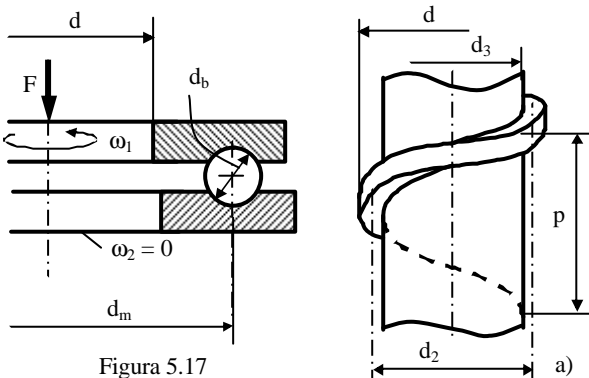


Figura 5.17

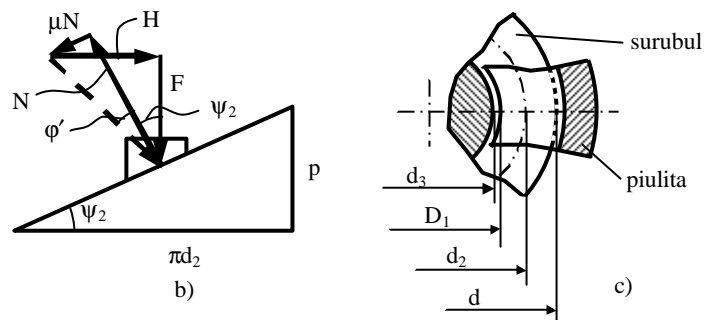


Figura 5.18

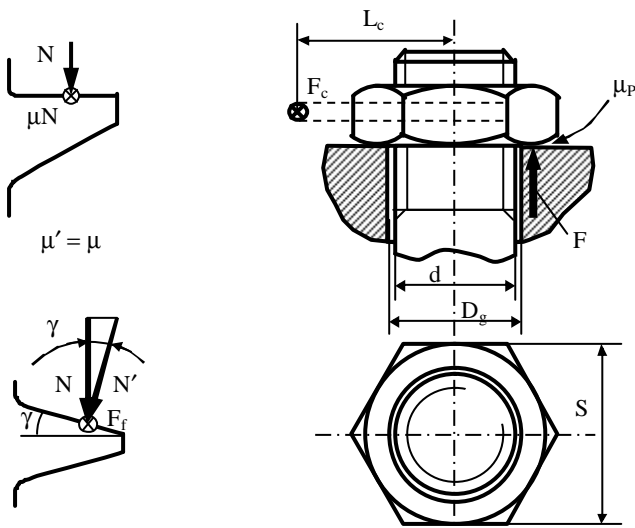


Figura 5.19

Figura 5.20

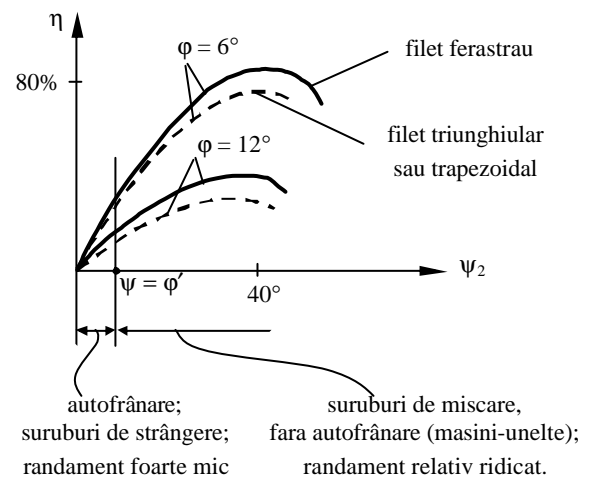


Figura 5.21

$$p_m = \frac{4 \cdot F}{\pi \cdot (d^2 - D_1^2)} \leq p_a \quad (5.77)$$

$$H = F \cdot \operatorname{tg}(\psi_2 + \phi'), \text{ unde } \psi_2 = \operatorname{arc} \operatorname{tg} \frac{p}{\pi \cdot d_2} \quad (5.78)$$

$$M_{t1} = H \cdot \frac{d_2}{2} = F \cdot \frac{d_2}{2} \cdot \operatorname{tg}(\psi_2 + \phi') \quad (5.79)$$

$$M'_{t1} = F \cdot \frac{d_2}{2} = F \cdot \frac{d_2}{2} \cdot \operatorname{tg}(\psi_2 - \phi') \quad (5.80)$$

$$\text{Punând condiția ca } M'_{t1} \leq 0, \text{ rezulta condiția de autofrânare } \psi_2 \leq \phi' \quad (5.81)$$

$$M_2 = \frac{1}{3} \cdot \mu_p \cdot F \cdot \frac{S^3 - D_g^3}{S^2 - D_g^2} \quad (5.82)$$

$$M_{\text{cheie}} = F \cdot \frac{d_2}{2} \cdot \operatorname{tg}(\psi_2 + \phi') + \frac{1}{3} \cdot \mu_p \cdot F \cdot \frac{S^3 - D_g^3}{S^2 - D_g^2} \quad (5.83)$$

$$\text{Pentru o cheie de lungime } L_c \text{ rezulta forța la cheie } F_{\text{cheie}} = \frac{M_{\text{cheie}}}{L_c}.$$

$$\text{Pentru o lungime standardizată } L_c = (12 \dots 15) \cdot d, \text{ rezulta } F \cong (60 \dots 100) \cdot F_{\text{cheie}}!$$

$$\eta = \frac{L_u}{L_c} = \frac{F \cdot p}{H \cdot \pi \cdot d_2} = \frac{F \cdot \operatorname{tg} \psi_2}{F \cdot \operatorname{tg}(\psi_2 + \phi')} = \frac{\operatorname{tg} \psi_2}{\operatorname{tg}(\psi_2 + \phi')} \quad (5.84)$$

$$\text{Punând condiția } \frac{d\eta}{d\psi} = 0 \text{ pentru randamentul maxim } \eta_{\max}, \text{ rezulta } \psi_{\text{opt}} = \frac{\pi}{4} - \frac{\phi'}{2} \cong 41^\circ \dots 42^\circ.$$

$$\eta = \frac{\operatorname{tg} \psi_2}{\operatorname{tg} 2 \cdot \psi_2} = \frac{\operatorname{tg} \psi_2}{\frac{2 \cdot \operatorname{tg} \psi_2}{1 - \operatorname{tg}^2 \psi_2}} = \frac{1 - \operatorname{tg}^2 \psi_2}{2} \leq 0,5! \quad (5.85)$$

$$\eta = \frac{M_{t1} \cdot 2 \cdot \pi}{(M_{t1} + M_2) \cdot 2 \cdot \pi} = \frac{F \cdot \frac{d_2}{2} \cdot \operatorname{tg} \psi_2}{F \cdot \left[ \frac{d_2}{2} \cdot \operatorname{tg}(\psi_2 + \phi') + \frac{1}{3} \cdot \mu_p \cdot \frac{S^3 - D_g^3}{S^2 - D_g^2} \right]} \text{ sau} \quad (5.86)$$

$$\eta = \frac{\operatorname{tg} \psi_2}{\operatorname{tg}(\psi_2 + \phi') + \frac{2}{3} \cdot \mu_p \cdot \frac{S^3 - D_g^3}{d_2 \cdot (S^2 - D_g^2)}} \quad (5.87)$$

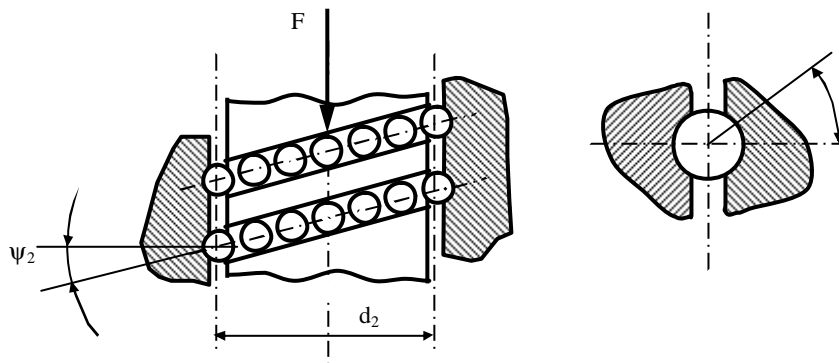


Figura 5.22

$$M_t = F \cdot \frac{d_2}{2} \cdot \operatorname{tg}(\psi_2 + \phi_r) \quad (5.88)$$

$$\text{Momentul este similar cu cel al cuplei surub-piulita cu alunecare, iar unghiul de frecare redus este } \phi_r = \operatorname{arc} \operatorname{tg} \frac{2 \cdot k}{d_2 \cdot \sin \gamma}.$$

În acest caz randamentul atinge valori de 80...85%, iar puterea pierdută prin frecare este de 50...100 de ori mai mică decât în cazul suruburilor cu alunecare.